

Managing FX Exposure

Transaction Exposure

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Class Announcements

- **Second Midterm:**

July 3 (6pm – 8pm). It will be run through Canvas.

- **First Midterm:**

Mean = 79 (Median = 81) & SD = 12.

Highest 97 – Lowest 54

⇒ Overall, a solid exam.

- **Next presentations:**

June 26 (Thursday) - Chapter 11

July 1 (Tuesday) - Chapter 16 (& maybe Chapter 17).

- **Second Midterm Review:** July 1.

Review: Exposure and NTE

- **Exposure (Risk)**

- At the firm level, currency risk is called *exposure*.

- **Three areas**

(1) *Transaction exposure*: Risk of transactions denominated in FC with a certain payment date or maturity.

(2) *Economic exposure*: Degree to which a firm's expected cash flows are affected by unexpected changes in S_t .

(3) *Translation exposure*: Accounting-based changes in a firm's consolidated statements that result from a change in S_t . Translation rules create accounting gains/losses due to changes in S_t .

We say a firm is “*exposed*” or has *exposure* if it faces currency risk.

Example: Exposure.

A. *Transaction exposure*.

Swiss Cruises, a Swiss firm, sells cruise packages priced in USD to a broker. Payment in 30 days.

B. *Economic exposure*.

Swiss Cruises has 50% of its revenue denominated in USD and only 20% of its cost denominated in USD. A depreciation of the USD will affect future CHF cash flows.

C. *Translation exposure*.

Swiss Cruises obtains a USD loan from a U.S. bank. This liability has to be translated into CHF following Swiss accounting rules. ¶

Review: Exposure and NTE

- Transaction exposure (TE) is easy to identify and measure.
 - Identification: Transactions denominated in FC with a **fixed** future date
 - Measure: Translate identified FC transactions to DC using S_t .

$$TE_{j,t} = \text{Value of a fixed future transaction in FC}_j * S_t$$

Example: Swiss Cruises.

Sold cruise packages for USD 2.5 million. Payment: 30 days.

Bought fuel oil for USD 1.5 million. Payment: 30 days.

$S_t = 1.45 \text{ CHF/USD}$.

Thus, the net transaction exposure in USD 30 days is:

$$\begin{aligned} \text{Net } TE_{j=USD} &= (\text{USD } 2.5\text{M} - \text{USD } 1.5\text{M}) * 1.45 \text{ CHF/USD} \\ &= \text{USD } 1\text{M} * 1.45 \text{ CHF/USD} = \text{CHF } 1.45\text{M}. \quad \P \end{aligned}$$

Managing TE

• A Comparison of External Hedging Tools

Transaction exposure: Risk from the settlement of transactions denominated in foreign currency.

Example: Imports, exports, acquisition of foreign assets.

- Organizational Tools to manage TE (Internal Methods):
 - Contracts that limit TE (Risk shifting (pricing in DC), Risk sharing)
 - Leading-lagging payments between subsidiaries
 - Inflows/Outflows Matching
- Financial Tools to manage TE (External Methods):
 - Futures/forwards (FH)
 - Options (OH)
 - Money market (MMH)

External Methods (Market-based Tools)

- **Review from Chapter 5 (FX Hedging Tools)**
- **Hedging Market-based Tools:**
 - ♦ **Futures/Forward:** Completely eliminates uncertainty
 - ◊ UP: *short* in the foreign currency.
HP: **long** in currency futures.
 - ◊ UP: *long* in the foreign currency.
HP: **short** in currency futures.
 - ♦ **Options:** Reduces uncertainty. How much? It depends on **X**.
 - ◊ UP: *short* in the foreign currency.
HP: **long** in currency **calls**.
 - ◊ UP: *long* in the foreign currency.
HP: **long** in currency **puts**.

- New tool: MMH

Money market hedge: Based on a replication of IRPT arbitrage.

Let's take the case of **receivables** denominated in FC:

- 1) **Borrow FC**
- 2) Convert to DC
- 3) Deposit DC in domestic bank
- 4) **Transfer FC receivable** to cover loan (+ interest) from (1).

Under IRPT, step 4) involves buying FC forward, to repay loan in (1)

⇒ This step is not needed, instead, we just transfer the FC receivable.

• New tool: MMH

Now, let's take the case of *payables* denominated in FC:

- 1) **Borrow DC**
- 2) Convert to FC
- 3) Deposit FC in domestic bank
- 4) **Transfer FC deposit** (+ interest) to cover payable in FC.

Under IRPT, step 4) involves selling FC/buying DC forward, to repay loan in (1)

⇒ This step is not needed, instead, we just transfer the FC deposit.

Q: Why MMH instead of FH?

- Under perfect markets ⇒ MMH = FH
- Under less than perfect markets ⇒ MMH ≠ FH

• **Comparison of Hedging Strategies**

Example: Iris Oil Inc. has a large FC exposure in the form of a CAD cash flow from its Canadian operations. Iris decides to transfer **CAD 300M** to its USD account in 90 days.

FX risk to Iris: CAD may depreciate against the USD.

Data:

$S_t = 0.8451 \text{ USD/CAD}$

$F_{t,90\text{-day}} = 0.8493 \text{ USD/CAD}$

$i_{\text{USD}} = 3.92\%$

$i_{\text{CAD}} = 2.03\%$

<u>X</u>	<u>Calls</u>	<u>Puts</u>
.82 USD/CAD	----	0.21
.84 USD/CAD	1.58	0.68
.88 USD/CAD	0.23	----

Example (continuation):

<u>Date</u>	<u>Spot market</u>	<u>Forward market</u>	<u>Money market</u>
t	$S_t = .8451 \text{ USD/CAD}$	$F_{t,T=90\text{-day}} = .8493 \text{ USD/CAD}$	$i_{\text{USD}} = 3.92\%$ $i_{\text{CAD}} = 2.03\%$

$t + 90$ Receive **CAD 300M** and transfer into USD.

$$\text{NTE} = \text{CAD } 300\text{M} * .8451 \text{ USD/CAD} = \text{USD } 253.53\text{M}$$

• **Hedging Strategies:**

1. Do Nothing

Do not hedge and exchange the **CAD 300M** at S_{t+90} .

2. Forward Market

At t , sell the **CAD 300M** forward and at time $t + 90$ guarantee:

$$\text{CAD } 300\text{M} * .8493 \text{ USD/CAD} = \text{USD } 254,790,000$$

Example (continuation):

3. Money Market

At t , Iris Oil takes the following three steps, simultaneously:

1) Borrow from Canadian bank at **2.03%** for 90 days :

$$\text{CAD } 300\text{M} / [1 + .0203 * (90/360)] = \text{CAD } 298,485,188.$$

2) Convert to USD at S_t :

$$\text{CAD } 298,485,188 * .8451 \text{ USD/CAD} = \text{USD } 252,249,832$$

3) Deposit in US bank at **3.92%** for 90 days to guarantee at time $t+90$:

$$\text{USD } 252,249,832 * [1 + .0392 * (90/360)] = \text{USD } 254,721,880.$$

Note: Both the FH and the MMH guarantee certainty at time $t+90$

FH delivers to Iris Oil: **USD 254,790,000**

MMH delivers to Iris Oil: **USD 254,721,880**

\Rightarrow Iris Oil selects the FH. (MMH is a *dominated* strategy.)

Example (continuation):**4. Option Market**

At t , buy a **put**. Available 90-day options:

Σ	Calls	Puts
.82 USD/CAD	----	0.21
.84 USD/CAD	1.58	0.68
.88 USD/CAD	0.23	----

Buy the **.84 USD/CAD put** \Rightarrow Total premium cost of **USD 2.04M**.

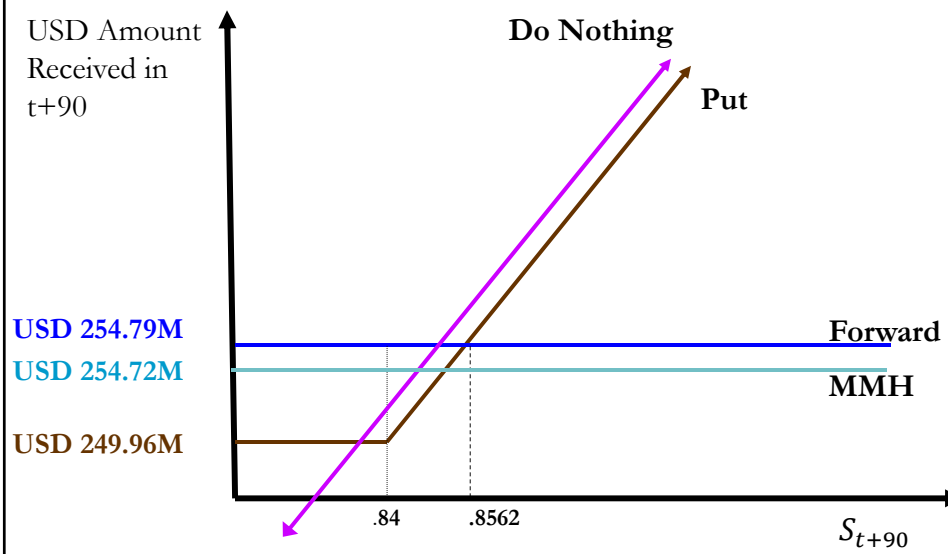
Position	Initial CF	Cash flows at $t+90$	
		$S_{t+90} < .84 \text{ USD/CAD}$	$S_{t+90} > .84 \text{ USD/CAD}$
Option (HP)	USD 2.04M	$(.84 - S_{t+90}) * \text{CAD } 300\text{M}$	0
Underlying (UP)	0	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$
Total CF	USD 2.04M	USD 252M	$S_{t+90} \text{ CAD } 300\text{M}$

Net CF at $t + 90$:

USD 249,960,000 for $S_{t+90} < .84 \text{ USD/CAD}$
 or $S_{t+90} * \text{CAD } 300\text{M} - \text{USD } 2.04\text{M}$ for $S_{t+90} > .84 \text{ USD/CAD}$

Example (continuation):

- Let's plot all strategies:



Example (continuation): Companies do not like paying premiums.

5. Collar

At time t , *buy* a **put** and *sell* a **call**.

Buy **.84** put at **USD 0.0068**

Sell **.88** call at **USD 0.0023**. \Rightarrow Initial cost = **USD 0.0045** per collar

\Rightarrow Total cost: **USD 1.35M**

Position	Initial CF	Cash flows at $t+90$		
		$S_{t+90} < .84$	$.84 < S_{t+90} < .88$	$S_{t+90} > .88$
Put	USD 2.04M	$(.84 - S_{t+90}) * \text{CAD } 300\text{M}$	0	0
Call	-USD 0.69M	0	0	$(.88 - S_{t+90}) * \text{CAD } 300\text{M}$
UP	0	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$	$S_{t+90} * \text{CAD } 300\text{M}$
Total CF	USD 1.35M	USD 252M	$S_{t+90} \text{ CAD } 300\text{M}$	USD 264M

Net CF at $t + 90$:

USD 250.65M for $S_{t+90} < .84 \text{ USD/CAD}$

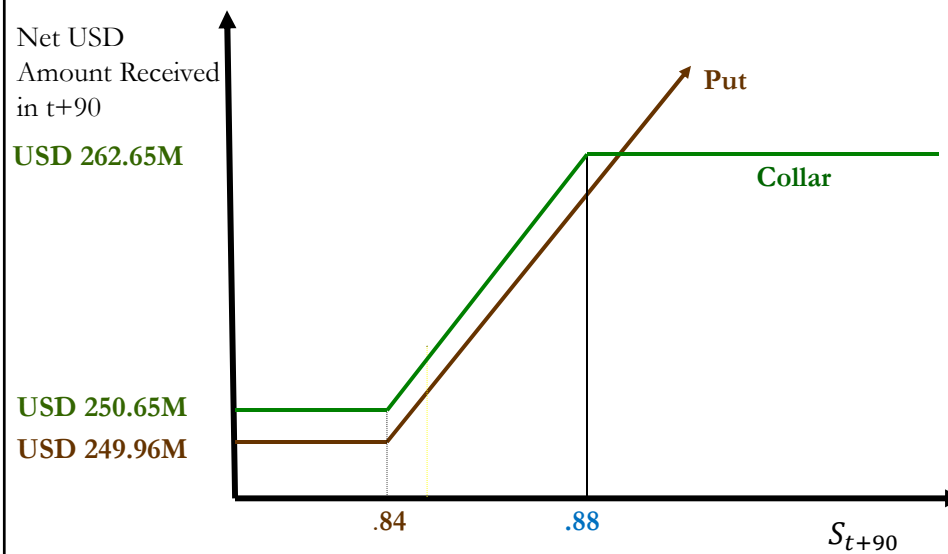
or $S_{t+90} \text{ CAD } 300\text{M} - \text{USD } 1.35\text{M}$ for $.84 \text{ USD/CAD} < S_{t+90} < .88 \text{ USD/CAD}$

or **USD 262.65M** for $S_{t+90} > .88 \text{ USD/CAD}$

Note: This collar reduces the upside: establishes a floor and a cap.

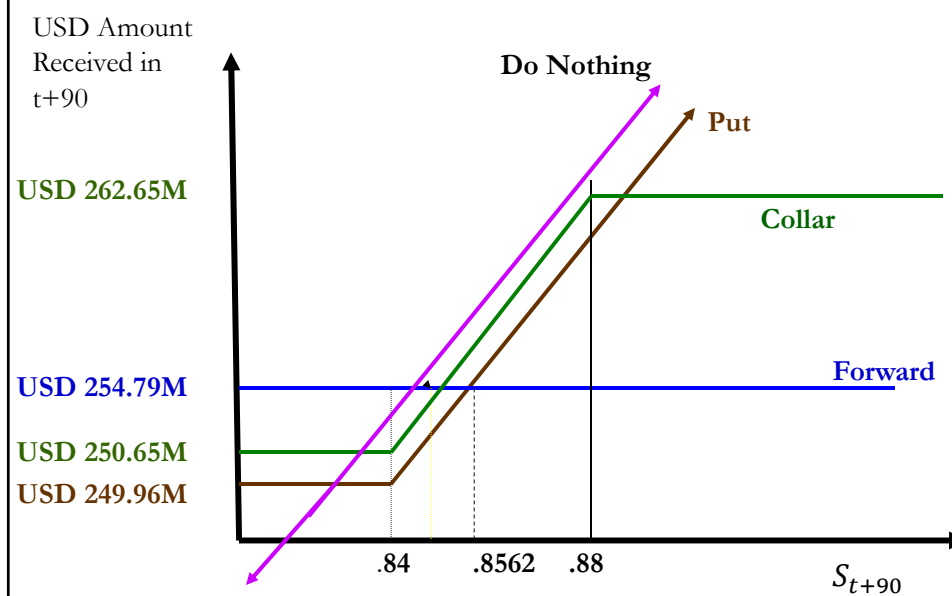
Example (continuation):

Let's plot the Collar and Put option strategies together. Relative to the put, the Collar limits the upside: The best case scenario is **USD 262.65M** (when sold put is exercised).



Example (continuation):

Let's plot all strategies:

**Managing TE – Hedging with FX Options****•Review: Reading Newspaper Quotes****PHILADELPHIA OPTIONS**

Wednesday, March 21, 2022

(PHLX is the exchange)

(Trading Date)

⇒ (Contracts traded)

⇒ (Vol=Volume, Last=Premium)

⇒ ($S_t = .7992$ USD/AUD)

⇒ (AUD 10,000 = Size, prices in USD cents)

		Calls		Puts	
		Vol.	Last	Vol.	Last

Australian Dollar**79.92****10,000 Australian Dollars-cents per unit.**

78	June	9	3.37	20	1.49
79	April	20	1.79	16	0.88
80	May	15	1.96	8	2.05
80	June	11	2.29	9	2.52
82	June	1	1.38	2	3.61

↑

↑

↑

↑

X=Strike T=Maturity Call Premium Put Premium

Price

• **Receivables in FC**

Example : Receivables AUD 20M \Rightarrow Hedge with **FX puts**

OTM: $X_{\text{put-June}} = 0.78 \text{ USD/AUD}$, $P = \text{USD } .0149$

Cost = Total premium = $\text{AUD } 20\text{M} * \text{USD } .0149/\text{AUD} = \text{USD } 298\text{K}$

Floor = $0.78 \text{ USD/AUD} * \text{AUD } 20\text{M} = \text{USD } 15.6\text{M}$ (Net: **USD 15.302M**)

ITM: - $X_{\text{put-June}} = 0.82 \text{ USD/AUD}$, $P = \text{USD } .0361$

- $X_{\text{put-June}} = .80 \text{ USD/AUD}$, $P = \text{USD } .0252$ (almost ATM)

• $X_{\text{put-June}} = 0.82 \text{ USD/AUD}$

Cost = Total premium = $\text{AUD } 20\text{M} * \text{USD } .0361/\text{AUD} = \text{USD } 722\text{K}$

Net Floor = $0.82 \text{ USD/AUD} * \text{AUD } 20\text{M} - \text{USD } 722\text{K} = \text{USD } 15.678\text{M}$

• $X_{\text{put-June}} = 0.80 \text{ USD/AUD}$ (ATM option)

Cost = Total premium = **USD 504K**

Net Floor = $0.82 \text{ USD/AUD} * \text{AUD } 20\text{M} - \text{USD } 504\text{K} = \text{USD } 15.496\text{M}$

Note: The higher the cost, the higher the floor for the AUD 20M. ¶

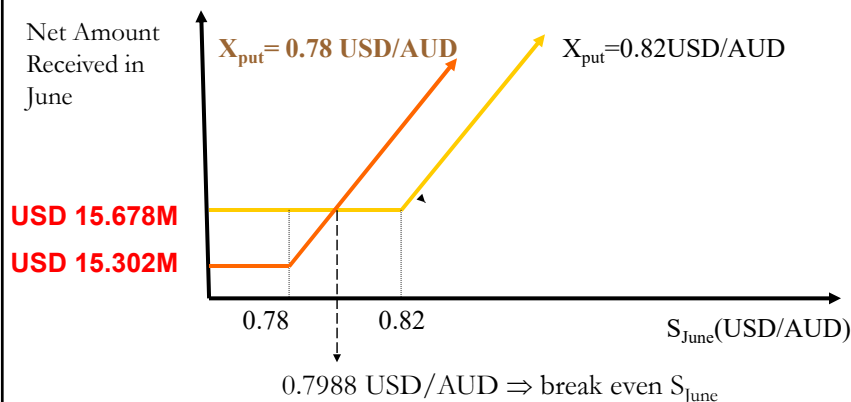
• All the FX options limit FX risk:

- $X_{\text{put-June}} = 0.78 \text{ USD/AUD} \Rightarrow$ Net floor: **USD 15.302M**

- $X_{\text{put-June}} = 0.80 \text{ USD/AUD} \Rightarrow$ Net floor: **USD 15.496M**

- $X_{\text{put-June}} = 0.82 \text{ USD/AUD} \Rightarrow$ Net floor: **USD 15.678M**

Q: Which one is better? It depends on your preferences and expectations.



Lesson from these examples:

- Options offer the typical insurance trade-off: Better coverage (lower cap, higher floor) \Rightarrow Higher cost (higher premium)
- Insurance is expensive. For the $X_{\text{put-June}} = 0.80 \text{ USD/AUD}$ case, it costs **USD .504M** to insure **USD 15.496M** (a 3.2% premium).

- We can lower the cost of insurance with a Collar, in this case: buy put & sell call, usually OTM.

Example: Buy $X_{\text{put-June}} = 0.78 \text{ USD/AUD}$ ($P = \text{USD .0149}$)
 Sell $X_{\text{call-June}} = .82 \text{ USD/AUD}$ ($P = \text{USD .0138}$)

Cost = $\text{USD .0149} * 20\text{M} - \text{USD .0138} * 20\text{M} = \text{USD } 22\text{K}$ (very low!)

Net Floor = $0.78 \text{ USD/AUD} * \text{AUD } 20\text{M} - \text{USD .022M} = \text{USD } 15.578\text{M}$

Net Cap = $0.82 \text{ USD/AUD} * \text{AUD } 20\text{M} - \text{USD .022M} = \text{USD } 16.378\text{M}$

A collar is cheaper, but it limits the upside of the option. ¶

- Payables in FC**

Example: Payable **AUD 100M** in Mid-June \Rightarrow Hedge with **FX calls**

$S_t = .7992 \text{ USD/AUD}$

$X_{\text{call-June}} = .78 \text{ USD/AUD}$, $P = \text{USD .0337}$

$X_{\text{put-June}} = .78 \text{ USD/AUD}$, $P = \text{USD .0149}$

$X_{\text{call-June}} = .80 \text{ USD/AUD}$, $P = \text{USD .0229}$

$X_{\text{put-June}} = .80 \text{ USD/AUD}$, $P = \text{USD .0252}$

$X_{\text{call-June}} = .82 \text{ USD/AUD}$, $P = \text{USD .0138}$

$X_{\text{put-June}} = .82 \text{ USD/AUD}$, $P = \text{USD .0361}$

OTM: - $X_{\text{call-June}} = 0.82 \text{ USD/AUD}$

- $X_{\text{call-June}} = 0.80 \text{ USD/AUD}$ ($\approx \text{ATM}$)

- $X_{\text{call-June}} = 0.82 \text{ USD/AUD}$, Premium = **USD .0138**

Cost = Total premium = **AUD 100M** * **USD .0138/AUD** = **USD 1.38M**

Cap = **AUD 100M** * **0.82 USD/AUD** = **USD 82M** (Net: **USD 83.38M**)

• $X_{\text{call-June}} = 0.80 \text{ USD/AUD}$, Premium = USD .0229 (almost ATM)
 Cost = Total premium = AUD 100M * USD .0229/AUD = USD 2.29M
 Net Cap = AUD 100M * 0.80 USD/AUD + USD 2.29M = USD 82.29M

ITM: $X_{\text{call-June}} = 0.78 \text{ USD/AUD}$, Premium = USD .0337

Cost = Total premium = USD 3.37M

Net Cap = AUD 100M * 0.78 USD/AUD + USD 3.37M = USD 81.37M

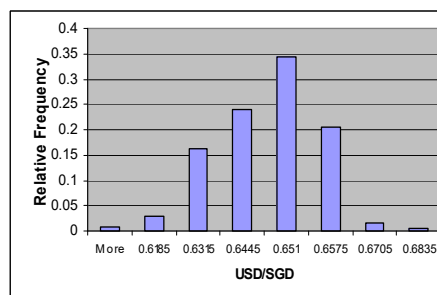
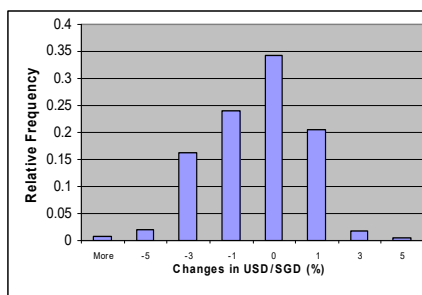
Note: The higher the cost, the lower the cap established for the AUD 100M payable.

Again, we can lower the cost of insurance using a Collar, in this case: buy a call & sell a put, usually, both OTM.¶

• Optimal Hedging Strategies?

Q: Which strategy is better? We need to say something about S_{t+T} . In the Iris Oil example, we need to make assumptions about S_{t+90} . For example, we can assume a distribution (normal) or use the ED to say something about future changes in S_t .

Example: Suppose we have a **receivable in SGD** in 30 days. We can use the **distribution** for monthly USD/SGD changes from the past 30 years. Then, we get the distribution for S_{t+30} (USD/SGD).



• **Examples assuming an explicit distribution for S_{t+T}**

Example – Receivables: Evaluate (1) FH, (2) MMH, (3) OH & (4) NH.

Cud Corp will receive **SGD 500,000** in 30 days. (SGD Receivable.)

Data:

- $S_t = .6500 - .6507 \text{ USD/SGD}$.
- $F_{t,T=30\text{-day}} = .6510 - .6519 \text{ USD/SGD}$.
- 30-day interest rates: $i_{\text{SGD}}: 2.65\% - 2.75\%$ & $i_{\text{USD}}: 3.20\% - 3.25\%$
- A 30-day put option on SGD: $X = .65 \text{ USD/SGD}$ and $P_t = \text{USD}.01$.
- Forecasted S_{t+30} :

Possible Outcomes	Probability
USD .63	18%
USD .64	24%
USD .65	34%
USD .66	21%
USD .68	3%

(1) FH: Sell SGD 30 days forward

$$\begin{aligned} \text{USD received in 30 days} &= \text{Receivables in SGD} * F_{t,30} \\ &= \text{SGD } 500,000 * .651 \text{ USD/SGD} = \text{USD } 325,500. \end{aligned}$$

(2) MMH:

- Borrow SGD at **2.75%** for 30 days,
- Convert to USD at **.65 USD/SGD**,
- Deposit USD at **3.2%** for 30 days,
- Repay SGD loan in 30 days with SGD 500,000 receivable

$$\begin{aligned} \text{Amount to borrow} &= \text{SGD } 500,000 / (1 + .0275 * 30/360) = \\ &= \text{SGD } 498,856.79 \end{aligned}$$

$$\begin{aligned} \text{Convert to USD (Amount to deposit in U.S. bank)} &= \\ &= \text{SGD } 498,856.79 * .65 \text{ USD/SGD} = \text{USD } 324,256.91 \end{aligned}$$

$$\begin{aligned} \text{Amount received in 30 days from U.S. bank deposit} &= \\ &= \text{USD } 324,256.91 * (1 + .032 * 30/360) = \text{USD } 325,121.60 \end{aligned}$$

(3) OH: Purchase put option.

$$X = .65 \text{ USD/CHF}$$

$$P_t = \text{premium} = \text{USD } .01$$

Possible S_{t+30}	Premium per SGD + Op Cost	Exercise?	Net USD Received for SGD 0.5M	Prob
.63 USD/SGD	USD .010027	Yes	USD 319,986.5	18%
.64 USD/SGD	USD .010027	Yes	USD 319,986.5	24%
.65 USD/SGD	USD .010027	No	USD 319,986.5	34%
.66 USD/SGD	USD .010027	No	USD 324,986.5	21%
.68 USD/SGD	USD .010027	No	USD 334,986.5	3%

Note: In the Total Amount Received (in USD) we have subtracted the *opportunity cost* involved in the upfront payment of a premium:

$$\text{USD } .01 * .032 * 30/360 = \text{USD } .000027 \quad (\text{Total} = \text{USD } 13.50)$$

$$\Rightarrow \text{Total Premium Cost: USD } 5,013.50$$

$$E[\text{Amount Received in USD}] = 319,986.5 * .76 + 324,986.50 * .21 + 334,986.50 * .03 = \text{USD } 321,486.5$$

(4) No Hedge (NH): Sell SGD 500,000 in the spot market in 30 days.

Possible S_{t+30}	USD Received for SGD 0.5M	Probability
.63 USD/SGD	USD 0.315M	18%
.64 USD/SGD	USD 0.320M	24%
.65 USD/SGD	USD 0.325M	34%
.66 USD/SGD	USD 0.330M	21%
.68 USD/SGD	USD 0.340M	3%

Note: When we compare (1) to (4), it's not clear which one is better. Preferences will matter. We can calculate an expected value:

$$E[\text{Amount Received in USD}] = 315K * .18 + 320K * .24 + 325K * .34 + 330K * .21 + 335K * .03 = \text{USD } 323,500$$

Conclusion: Cud Corporation is likely to choose the FH. But, risk preferences matter. ¶

Example – Payables: Evaluate (1) FH, (2) MMH, (3) OH, (4) No Hedge

Situation: Cud Corp needs **CHF 100,000** in 180 days. (CHF Payable.)

Data:

- $S_t = .675 - .680 \text{ USD/CHF}$.
- $F_{t,180} = .695 - .700 \text{ USD/CHF}$.
- 180-day interest rates are as follows:
 $i_{\text{CHF}}: 9\% - 10\%;$
 $i_{\text{USD}}: 13\% - 14.0\%$
- A 180-day call option on CHF: $X = .70 \text{ USD/CHF}$ and $P_t = \text{USD}.02$.
- Cud forecasted S_{t+180} :

Possible Outcomes	Probability
USD .67	30%
USD .70	50%
USD .75	20%

(1) FH: Purchase CHF 180 days forward

$$\text{USD needed in 180 days} = \text{Payables in CHF} \times F_{t,180} \\ = \text{CHF } 100,000 * .70 \text{ USD/CHF} = \text{USD } 70,000.$$

(2) MMH:

- Borrow USD at **14%** for 180 days,
- Convert to CHF at **.680 USD/CHF**,
- Invest CHF at **9%** for 180 days,
- Repay USD loan in 180 days & transfer CHF deposit to cover payable

$$\text{Amount in CHF to be invested} = \text{CHF } 100,000 / (1 + .09 * 180/360) \\ = \text{CHF } 95,693.78$$

$$\text{Amount in USD needed to convert into CHF for deposit} = \\ = \text{CHF } 95,693.78 * .680 \text{ USD/CHF} = \text{USD } 65,071.77$$

$$\text{Interest and principal owed on USD loan after 180 days} = \\ = \text{USD } 65,071.77 * (1 + .14 * 180/360) = \text{USD } 69,626.79$$

- (3) OH: Purchase call option. $X = .70 \text{ USD/CHF}$
 $C_t = \text{premium} = \text{USD } .02.$

Possible S_{t+180}	Premium per CHF + Op Cost	Exercise?	Net Paid for CHF 0.1M	Prob
.67 USD/SGD	USD .0213	No	USD 69,130	30%
.70 USD/SGD	USD .0213	No	USD 72,130	50%
.75 USD/SGD	USD .0213	Yes	USD 72,130	20%

Note: In the Total USD Cost we have included the opportunity cost involved in the upfront payment of a premium = **USD 130**.

$$E[\text{Amount to Pay in USD}] = \text{USD } 69,130 * .30 + \text{USD } 72,130 * .70 \\ = \text{USD } 71,230$$

- *Preferences matter:* A risk taker may like the 30% chance of doing better with the OH than with the MMH.

- (4) Remain Unhedged: Purchase **CHF 100,000** in 180 days.

Possible S_{t+180}	Net Paid for CHF 0.1M	Probability
.67 USD/SGD	USD 67,000	30%
.70 USD/SGD	USD 70,000	50%
.75 USD/SGD	USD 75,000	20%

Preferences matter: Again, a risk taker may like the **30% chance** of doing better with the NH than with the MMH. (Actually, there is also an additional 50% chance of being very close to the MMH.)

$$E[\text{Amount to Pay in USD}] = \text{USD } 67,000 * .30 + \text{USD } 70,000 * .50 \\ + \text{USD } 75,000 * .20 = \text{USD } 70,100$$

Conclusion: Cud Corporation is likely to choose the MMH. ¶